

$$\mathcal{R} \cap \bigcap_{i=\alpha_j+1}^{\infty} a_i \sin(2\pi f x_i)$$